Tik-61.140 Signal Processing Systems

1st mid term exam, Mon 12.3.2001 15-18 K,L,N,T1. Simula/Koskela/Parviainen.

You may use a mathematical reference book (for example Beta) and a graphical calculator (clean memory). Some formulae in the additional paper. Write down your answers in concept papers.

- 1. (4p) LTI systems are by definition linear and time-invariant. A LTI system can be depicted with block diagram, difference equation or impulse response.
 - a) Explain briefly, in which way it is possible calculate or show that a given systems is linear and time-invariant.
 - b) Which of the following systems S_1 , S_2 , S_3 are linear and time-invariant? Explain your answers.

$$S_1: y[n] + 1 = x[n] + x[n-1]$$

 $S_2: y[n] = |x[n]|$
 $S_3: y(t) - tx(t) = 0$

- c) Sketch all block diagrams of LTI systems of b).
- 2. (3p) See Figure 1. There is an analog sum signal of two periodic cosine signals.

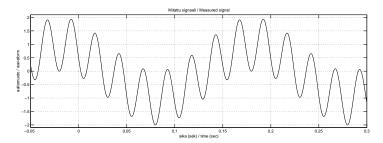


Figure 1: Sum signal

- a) What are the frequencies of two subsignals f_1 and f_2 ?
- b) What is the basic frequency f_0 of sum signal?
- c) Sketch the two-sided amplitude spectrum (energy of signal as a function of frequency) of sum signal in range $-50~{\rm Hz}$. 50 Hz. Alternatively, you can represent it with Fourier series and basic (angular) frequency, $\omega_0 = 2~\pi~f_0$.
- 3. (6p) Consider a LTI system with impulse response $h[n] = \delta[n] 2\delta[n-1] + \delta[n-2]$. In addition, it is known that it consists of two similar subsystems $h_1[n]$, which are set in cascade (series).
 - a) How long is impulse response $h_1[n]$.
 - b) Define the impulse response $h_1[n]$ of the subsystem.
 - c) Sketch the block diagram of system h[n].
 - d) Calculate the convolution x[n] * h[n], when x[n] is like in Figure 2.

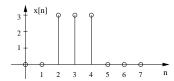


Figure 2: Input x[n]

4. (6p) Consider a continuous-time system whose frequency response is

$$H(j\omega) = \frac{e^{j\omega}}{2 + j\omega}$$

- a) Define the impulse response h(t) of the system.
- b) Suppose that the input is rectangular pulse $x(t) = \begin{cases} 1, & 0 < t < 2 \\ 0, & \text{muualla} \end{cases}$. Define the Fourier transform $Y(j\omega)$ of output.